

# Berkeley-Stanford Joint Algebraic Geometry Seminar

Tuesday, March 30, at Stanford

**Joe Harris**

Harvard

3:15–4:15, Rm. 383–N

**The Enriques conjecture; or, How canonical is the canonical bundle?**

**Abstract:** The question we're dealing with is this: Is there any way of associating to each smooth curve  $C$  of genus  $g$  — or at least to each  $C$  in an open subset of moduli — a line bundle on  $C$ , other than by taking powers of the canonical bundle? (The answer, by the way, is no: the canonical bundle is truly canonical.) This question was posed almost a century ago; a bogus proof was given by Franchetta in the '40s (as a result of which the statement is usually called *Franchetta's conjecture*), and a correct proof was given in the '80s by Harer and Mestrano, based on a topological argument of Harer's.

In fact, the statement is immediately implied by a stronger conjecture made by Enriques decades earlier. Enriques claimed (or suggested; it's not always clear) an analogous statement for the Severi variety, namely that the only ways of choosing a line bundle on a general plane curve  $C$  of degree  $d$  and genus  $g$  are combinations of the canonical bundle  $K_C$  and the hyperplane bundle  $\mathcal{O}_C(1)$ .

In this talk I'll discuss a little of the history of the Enriques conjecture, and variants of it; but the main purpose of the talk will be to give a proof of the conjecture that Deepee Khosla and I found recently.

**Mark de Cataldo**

Stony Brook

4:45–5:45, Rm. 383–N

**The Hodge theory of algebraic maps**

**Abstract:** I will discuss joint work with Luca Migliorini on new structures on the cohomology of projective manifolds.

**There will be a dinner afterward.**

This seminar alternates between Stanford and Berkeley. To organize transportation from Berkeley to Stanford, please contact David Eisenbud and Tom Graber.

<http://math.stanford.edu/~vakil/seminar0304/bs.html>