

section 4.5

2. we look for a particular solution $y(t) = ae^{-t}$. $a = (-3)/((-1)^2 + 6(-1) + 8) = -1$, thus $y(t) = -e^{-t}$
4. we look for a particular solution $y(t) = ae^{2t}$. $a = 18/(2^2 + 3 \cdot 2 - 18) = -9/4$
8. try $y(t) = a \cos 3t + b \sin 3t$. we have $-9a + 7 \cdot 3b + 10a = 0$ and $-9b - 7 \cdot 3a + 10b = -4$. $a = 42/221, b = -2/221$
12. $y(t) = -(21/100) \cos 2t + (3/100) \sin 2t$
18. the general solution for homogeneous equation is $y(t) = c_1 e^{-t} + c_2 e^{-2t}$ and we have a particular solution $y_p(t) = ae^{-4t}$ with $a = 3/((-4)^2 + 3(-4) + 2) = 1/2$. Initial conditions give $c_1 + c_2 + 1/2 = 1, -c_1 - 2c_2 - 2 = 0$, then $c_1 = 3, c_2 = -5/2$, therefore the solution is $3e^{-t} - \frac{5}{2}e^{-2t} + \frac{1}{2}e^{-4t}$
20. $y(t) = e^{-t}(c_1 \cos t + c_2 \sin t) + a \cos 2t + b \sin 2t$. We have $-4a + 4b + 2a = 2, -4b - 4a + 2b = 0$, implying $a = -1/5, b = 2/5$. Then $c_1 = -9/5, c_2 = -13/5$
26. $y(t) = t \sin 2t$

section 4.6

2. $y_p(t) = \frac{1}{2}t \sin 2t + \frac{1}{4} \ln(\cos 2t) \cos 2t$
6. $y_p(t) = \frac{1}{2}t^2 e^{2t}$
14. $y(t) = c_1 t^{-1} + c_2 t^{-1} \ln t + \frac{1}{2}t^{-1}(\ln t)^2$

section 4.7

10. $c_1 \cos 5t + c_2 \sin 5t + \frac{2}{5}t \sin(5t)$
12. $\frac{3}{2} \sin(2t)$
13. $-\frac{21}{130} \sin 4t - \frac{6}{65} \cos 4t$