Northern California Symplectic Geometry Seminar

Berkeley – Davis – Santa Cruz – Stanford

Monday, December 4, 2023 at Berkeley

2:30–3:30, room 736 EvansRohil Prasad (UC Berkeley)On the dense existence of compact invariant sets

Abstract: This is joint work in progress with Dan Cristofaro-Gardiner. We explore the topological dynamics of Reeb flows beyond periodic orbits and find the following rather general phenomenon. For any Reeb flow for a torsion contact structure on a closed 3-manifold, any point is arbitrarily close to a proper compact invariant subset of the flow. Such a statement is false if the invariant subset is required to be a periodic orbit. Stronger results can also be proved that parallel theorems of Le Calvez-Yoccoz, Franks, and Salazar for homeomorphisms of the 2-sphere. In fact, we can also extend their results to Hamiltonian diffeomorphisms of closed surfaces of any genus.

 $3{:}30{-}4{:}00$ — Tea Break

4:00–5:00, room 736 Evans Mohan Swaminathan (Stanford)

Constructing smoothings of stable maps

Abstract: The moduli space of closed holomorphic curves in a closed symplectic manifold can be compactified using stable maps. However, even in the nicest of situations (e.g., degree d curves of genus g in a complex projective space, with d ;; g), counting dimensions shows that most stable maps which have ghost components are not "smoothable", i.e., they can never appear as the limit of a sequence of non-singular holomorphic curves. It is therefore natural to ask which stable maps are smoothable (with the aim of obtaining a compact moduli space which is smaller than the full space of stable maps). In this talk, I will describe recent work (joint with Fatemeh Rezaee) which provides a partial answer to this question, in all genera, when the target is a smooth projective variety. We do this via a gluing construction, with the key new input being a class of explicit model solutions which dictate how to smooth a stable map near its ghost components.

There will be dinner in downtown Berkeley following the talks.

Organizers: M. Abouzaid, R. Casals, Y. Eliashberg, D. Fuchs, V. Ginzburg, M. Hutchings, E. Ionel, R. Montgomery, V. Shende, L. Starkston, K. Wehrheim, A. Weinstein