Abstract: I will discuss my approach towards the long-standing conjecture that $\pi_* L_{K(n)} S^0$ is a module of finite type over the $p$-adic integers. An important role is played by the action of the $n$th extended Morava stabilizer group on the spectrum $E_n$ and on the "continuous" homotopy fixed point spectra resulting from this action.