

(d) By part (c), we may take f and g as in (b). Then

(b) says Dirichlet composition in that case is direct composition. \square

(e) Let $M = f(1,1)g(1,1)$. By Exercise 2.18 $\exists x_0, y_0$ s.t.
 $\exists z_0, w_0$

$\gcd(f(x_0, y_0), M) = 1$, $\gcd(g(z_0, w_0), M) = 1$. Then

$F(x_0, y_0) = f(x_0, y_0)g(z_0, w_0)$ is prime to M as well.

$\left. \begin{array}{l} \\ \end{array} \right\}$
these are determined
by x_0, y_0, z_0, w_0

$F(1, 1) = f(1, 1)g(1, 1) = M$; so F represents M ;

by above arguments F represents an integer prime to M ,

therefore F has to be primitive as well.