

Rotational symmetry of self-similar solutions to the Ricci flow

Let (M, g) be a three-dimensional steady gradient Ricci soliton which is non-flat and κ -noncollapsed. We prove that (M, g) is isometric to the Bryant soliton up to scaling. This solves a problem mentioned in Perelman's first paper.